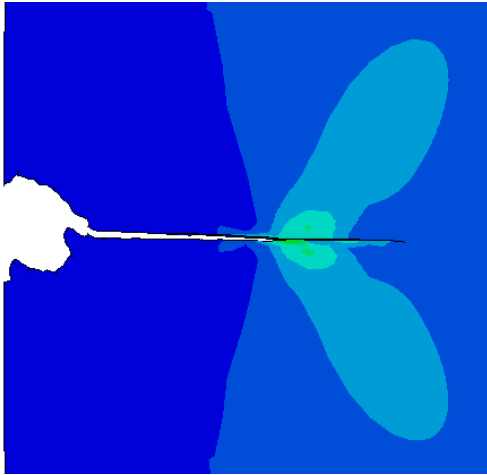
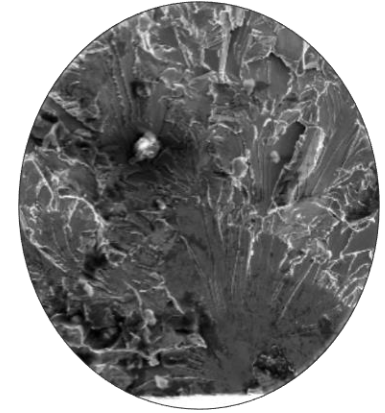
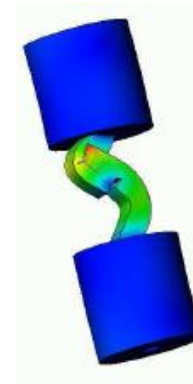


Exceptional service in the national interest



N=O=MAD



Project 4: Fatigue Behavior of Fe-Co-2V using Experimental, Computational, and Analytical Techniques

Students: Jacob Biddlecom, Benedict Pineyro, Matthew Mills

Mentors: Kyle Johnson, Scott Grutzik, Tariq Khraishi, Adam Brink, Matthew Brake

July 31, 2018

Mentors

Kyle Johnson (SNL)



Scott Grutzik (SNL)



Adam Brink (SNL)



Matthew Brake (Rice University)

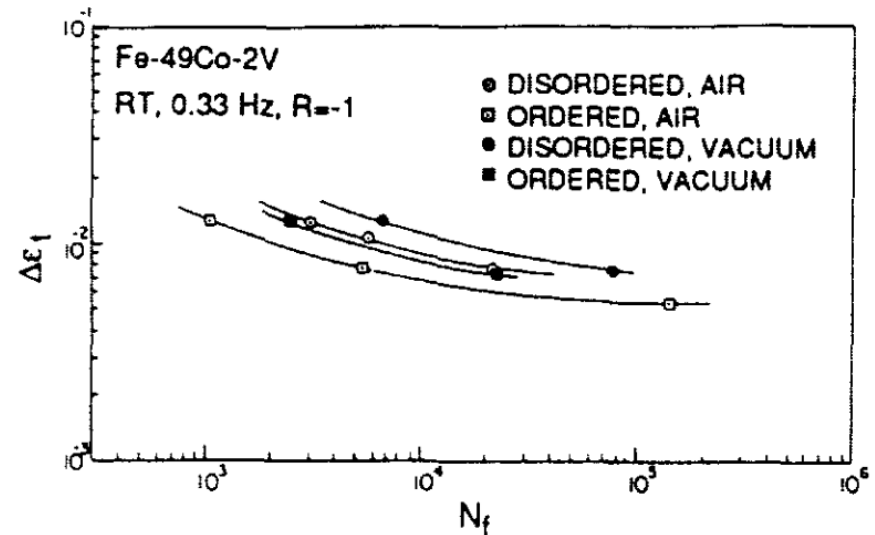
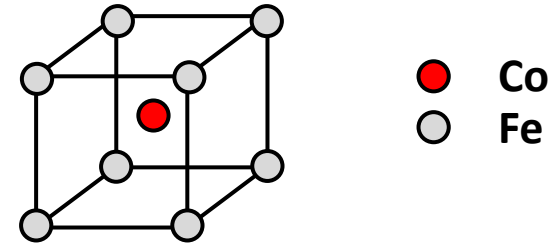


Tariq Khraishi (UNM)



Motivation

- Fe-Co-2V is soft, ferromagnetic material commonly used for electrical components
- Often exhibits low strength, poor ductility, and low workability due to an ordered B2 microstructure
- Limited fatigue data currently exists for Fe-Co-2V



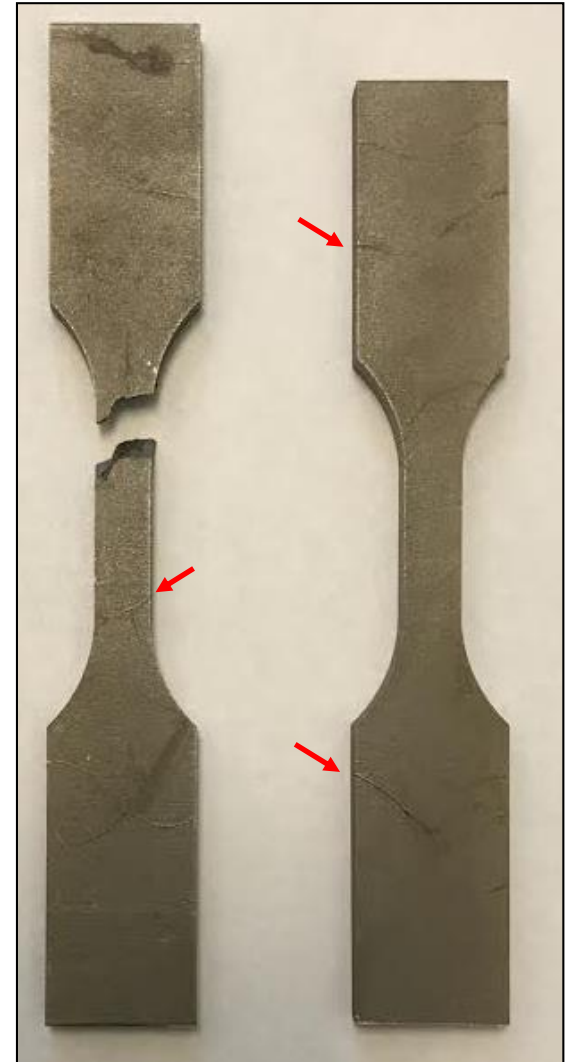
[Source: Stoloff et al., Scripta Metallurgica et Materialia, 1992]

Project Goal

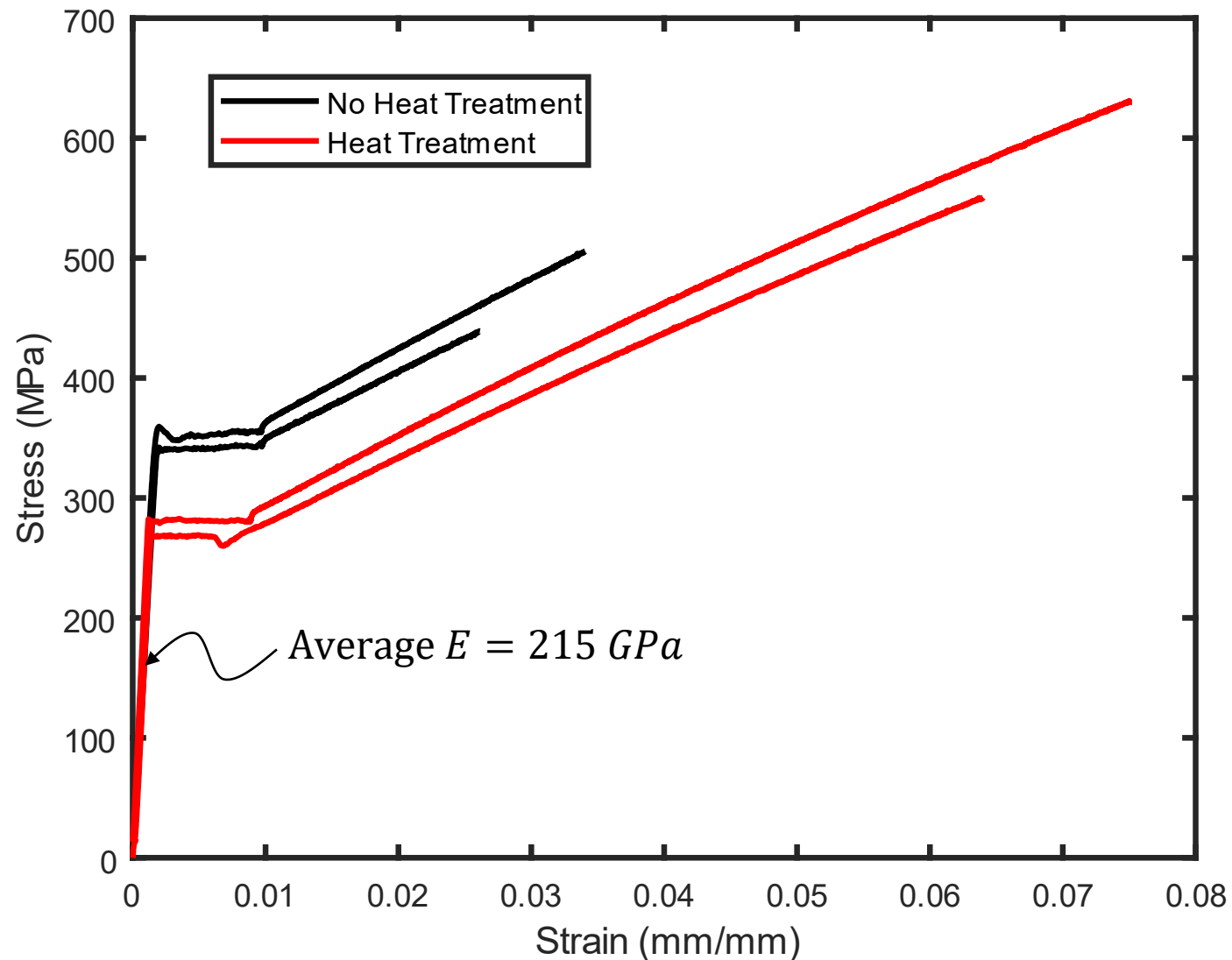
Characterize the fatigue properties of Fe-Co-2V through strain-controlled fatigue testing coupled with numerical and analytical modeling

Additively Manufactured (AM) Fe-Co-2V

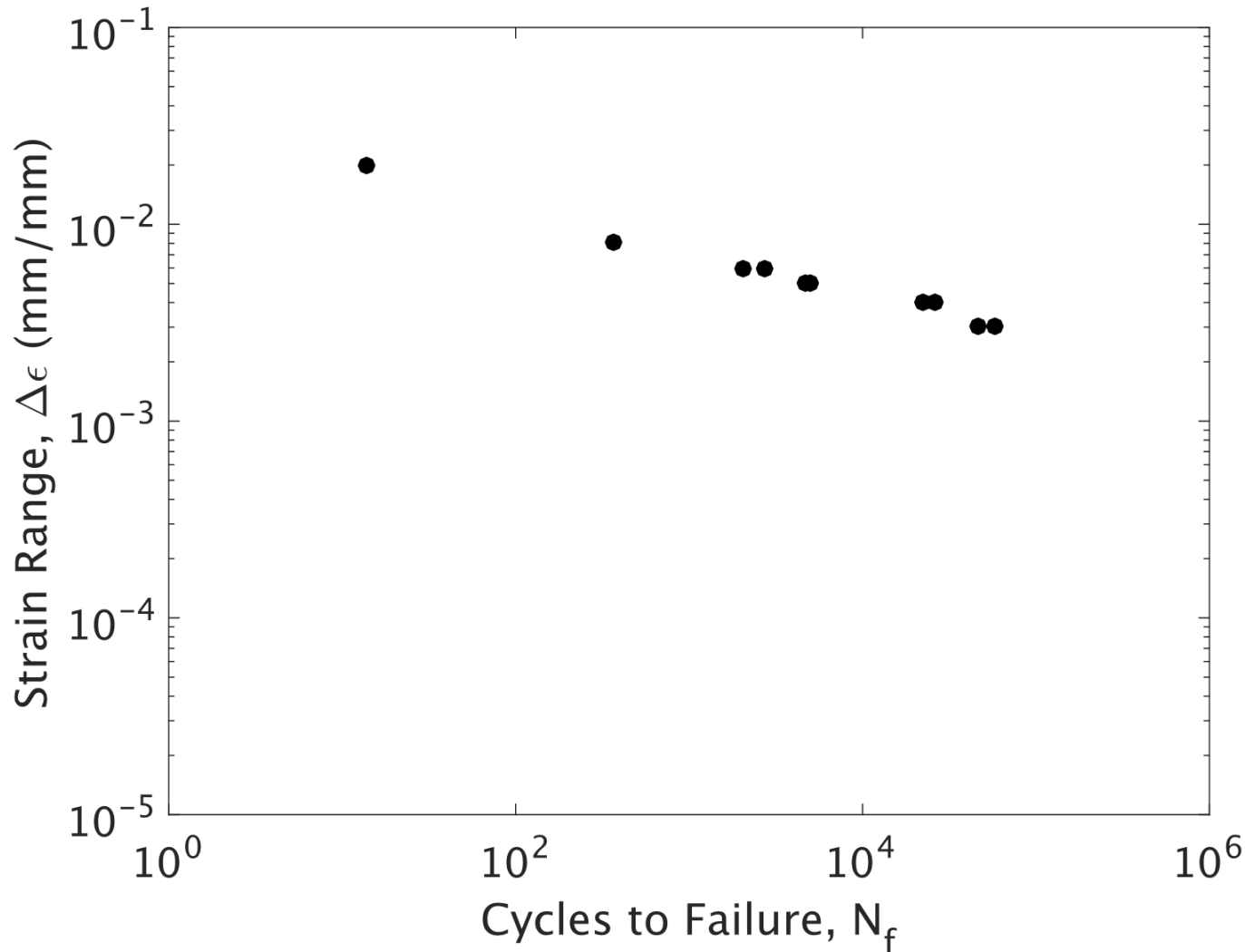
- Producing Fe-Co-2V using AM could potentially improve its mechanical properties
- AM Specimens exhibited significant cracking, likely from thermal residual stresses
- Proceeded to use wrought Fe-Co-2V for the study



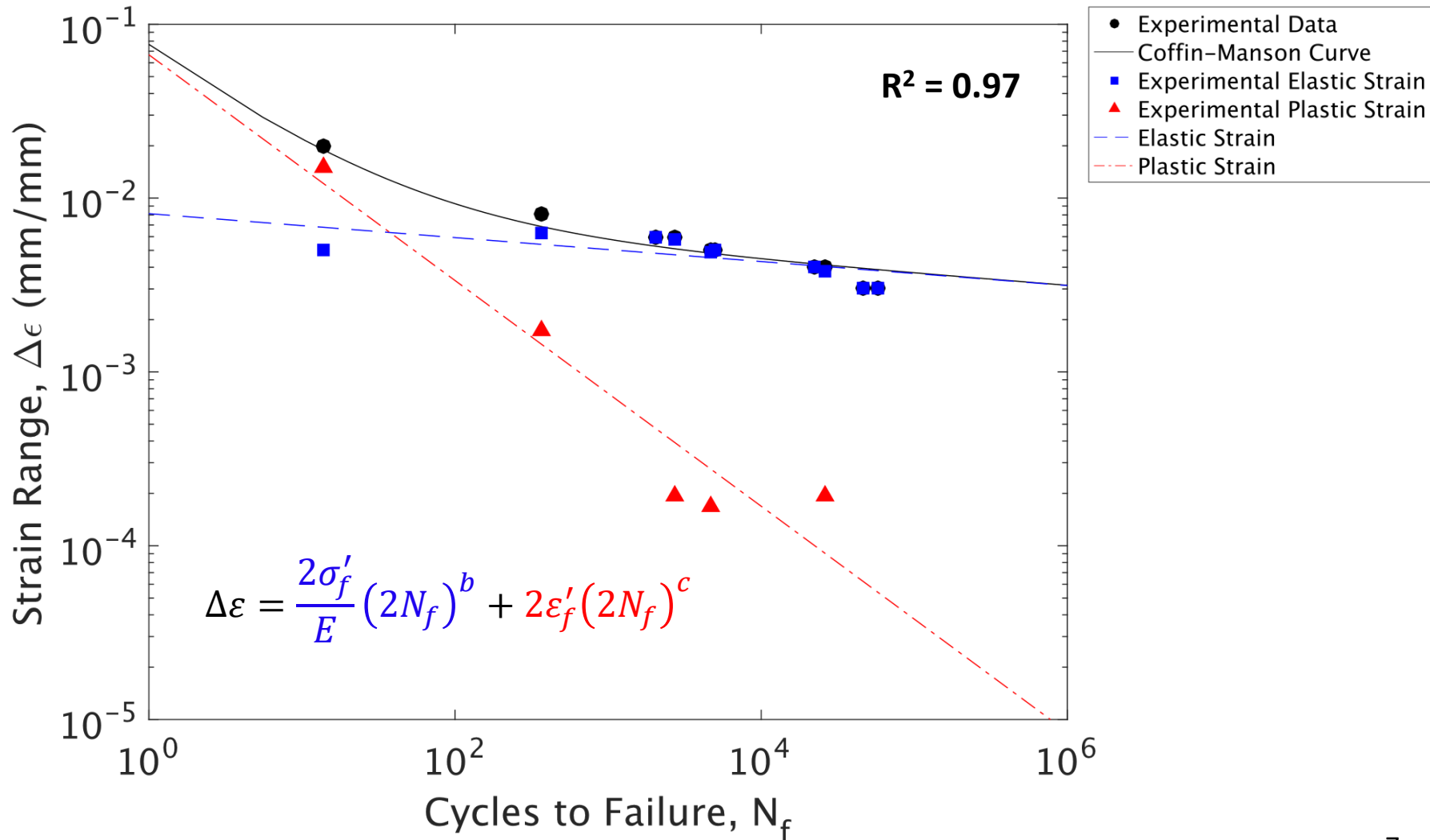
Quasi-Static, Monotonic Tension Tests



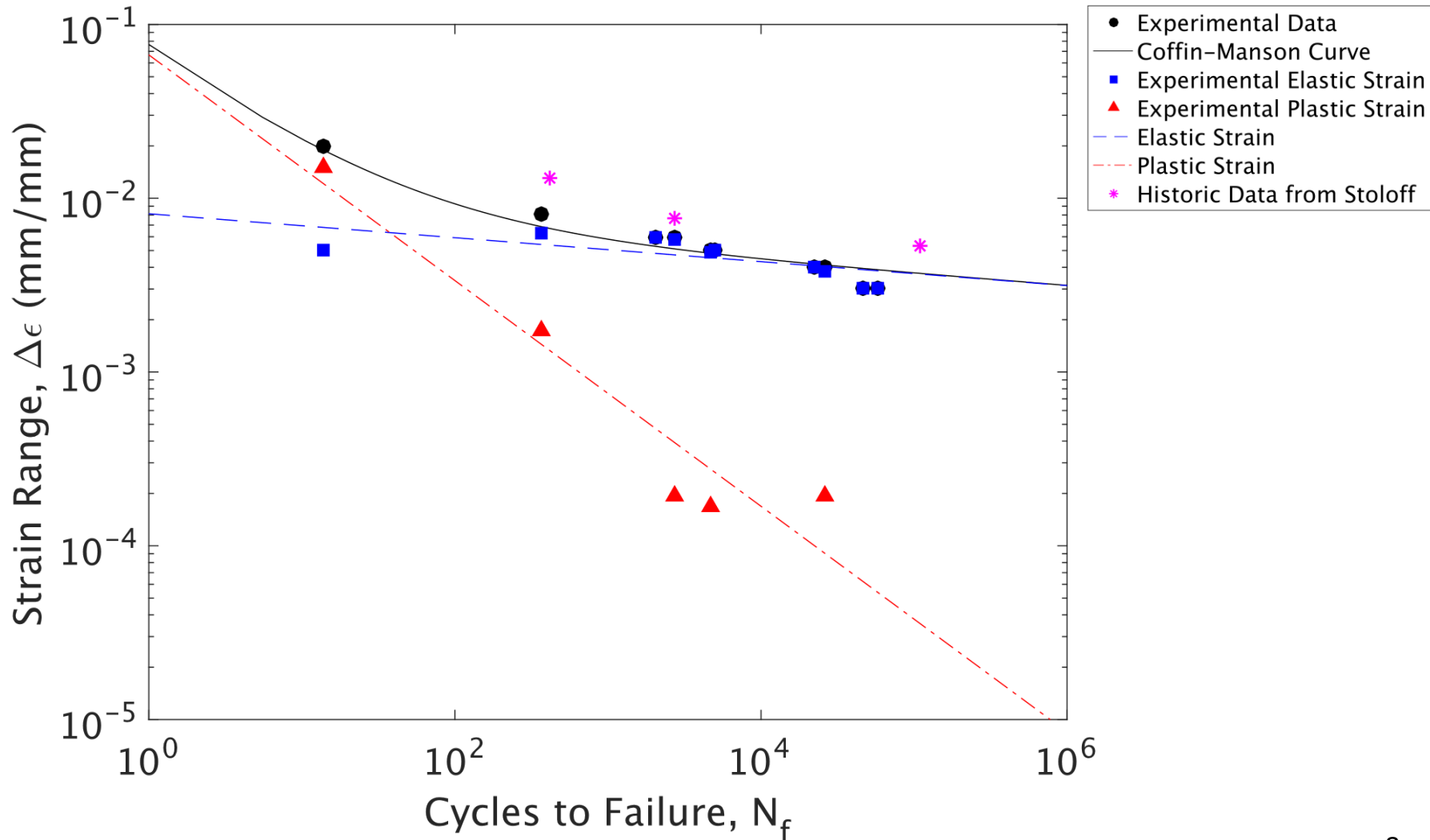
Strain-Controlled Fatigue Testing ($R=-1$, 1 Hz)



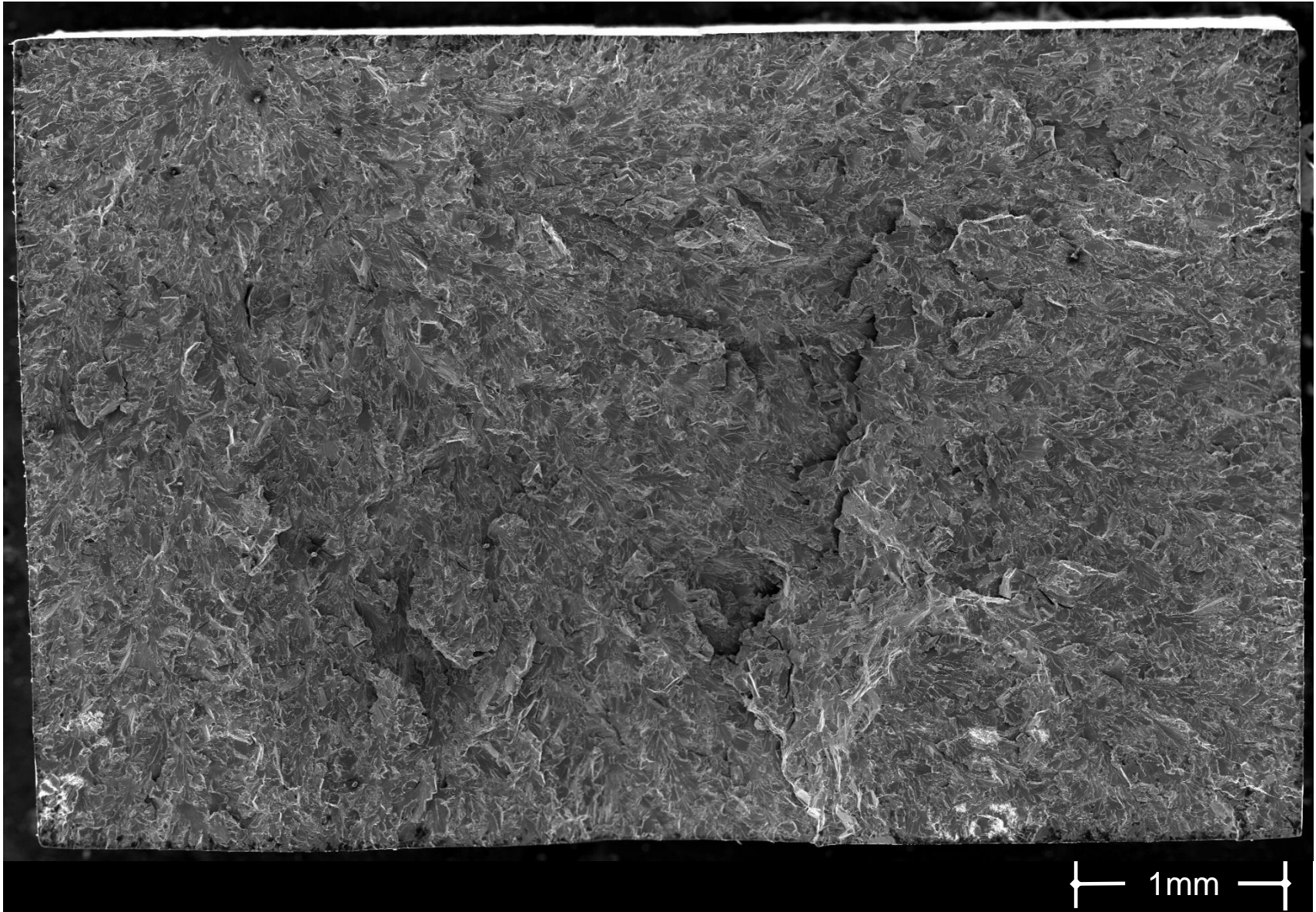
Strain-Controlled Fatigue Testing (R=-1, 1 Hz)



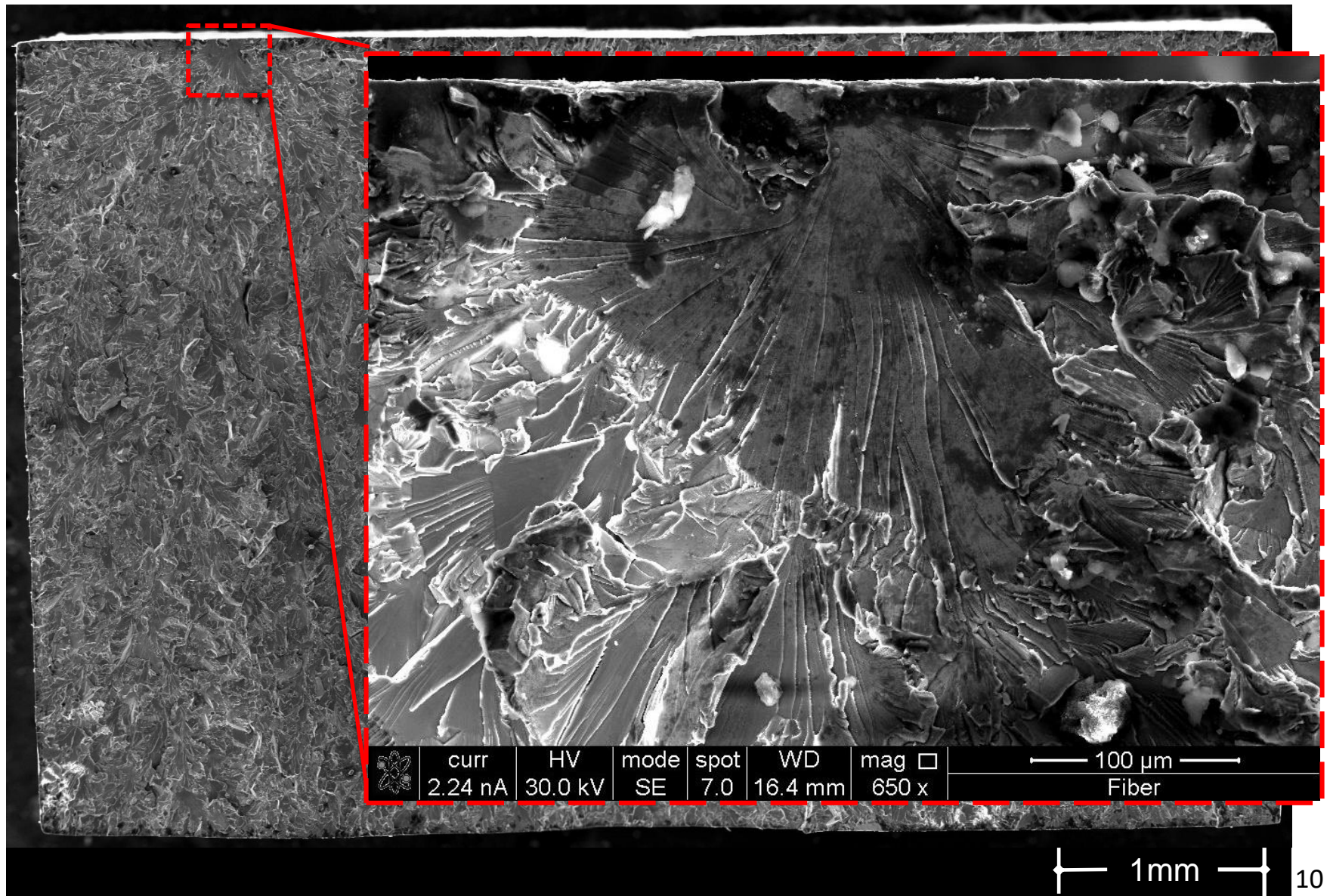
Strain-Controlled Fatigue Testing ($R=-1$, 1 Hz)



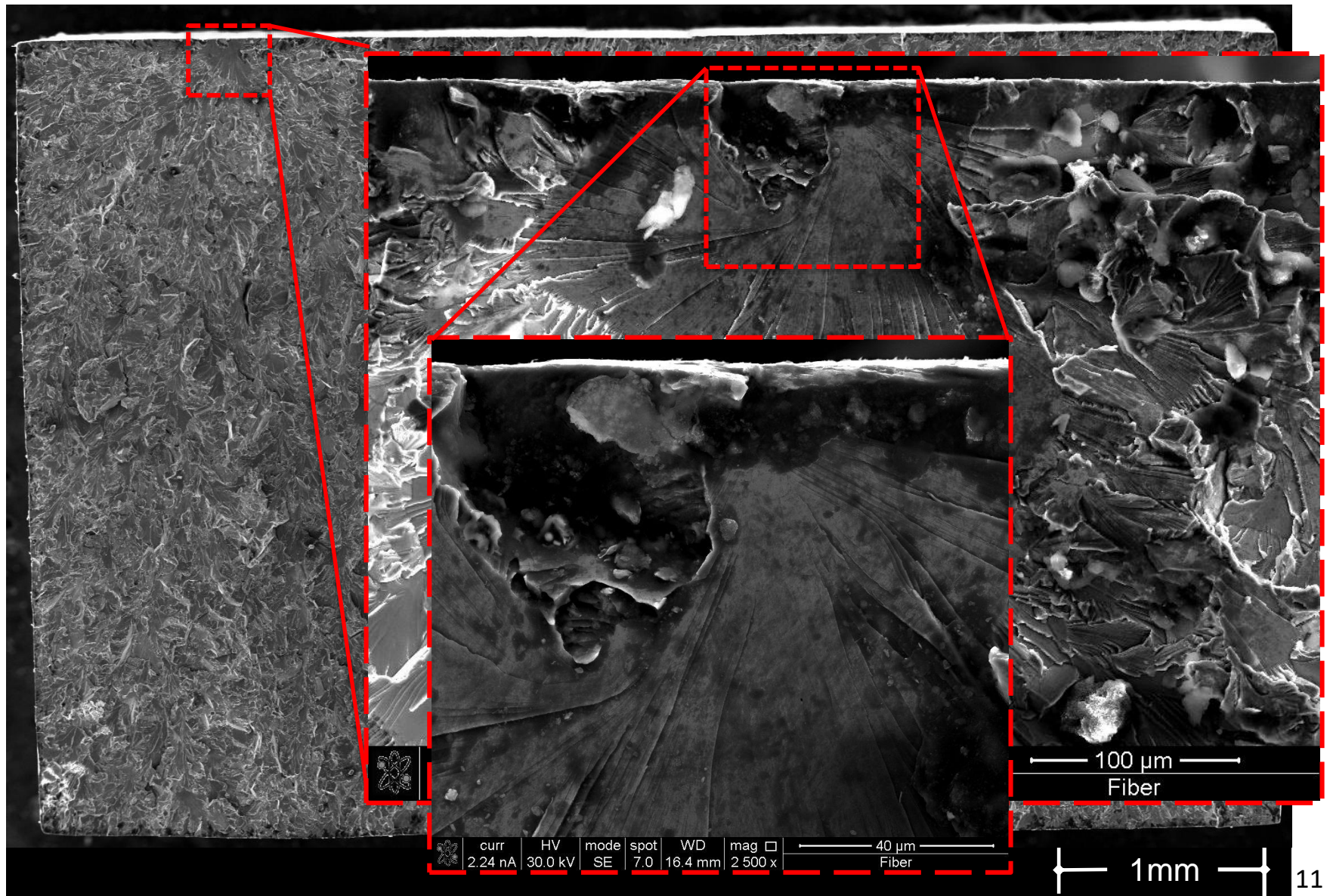
SEM – 1mm Scale



SEM – 100 μ m Scale



SEM – 40 μ m Scale



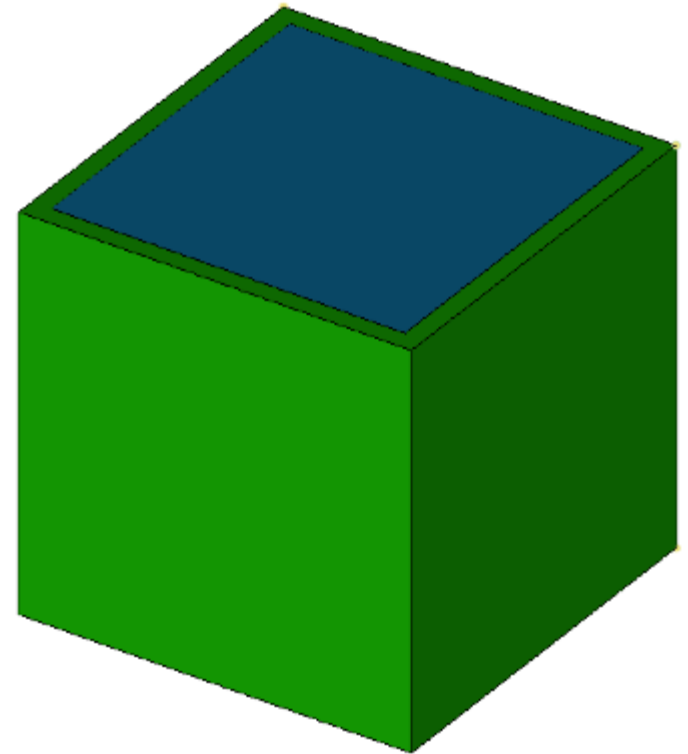
Calibration – Methods

- Gradient
 - Sequential Least Squared Programming (SLQSP)
 - Nelder-Mead
- Global
 - brute
 - basinhopping

Error Metric:

$$\text{MSE} = \frac{1}{n} \sum_{i=0}^n |f_i - y_i|^2$$

- Weighted function



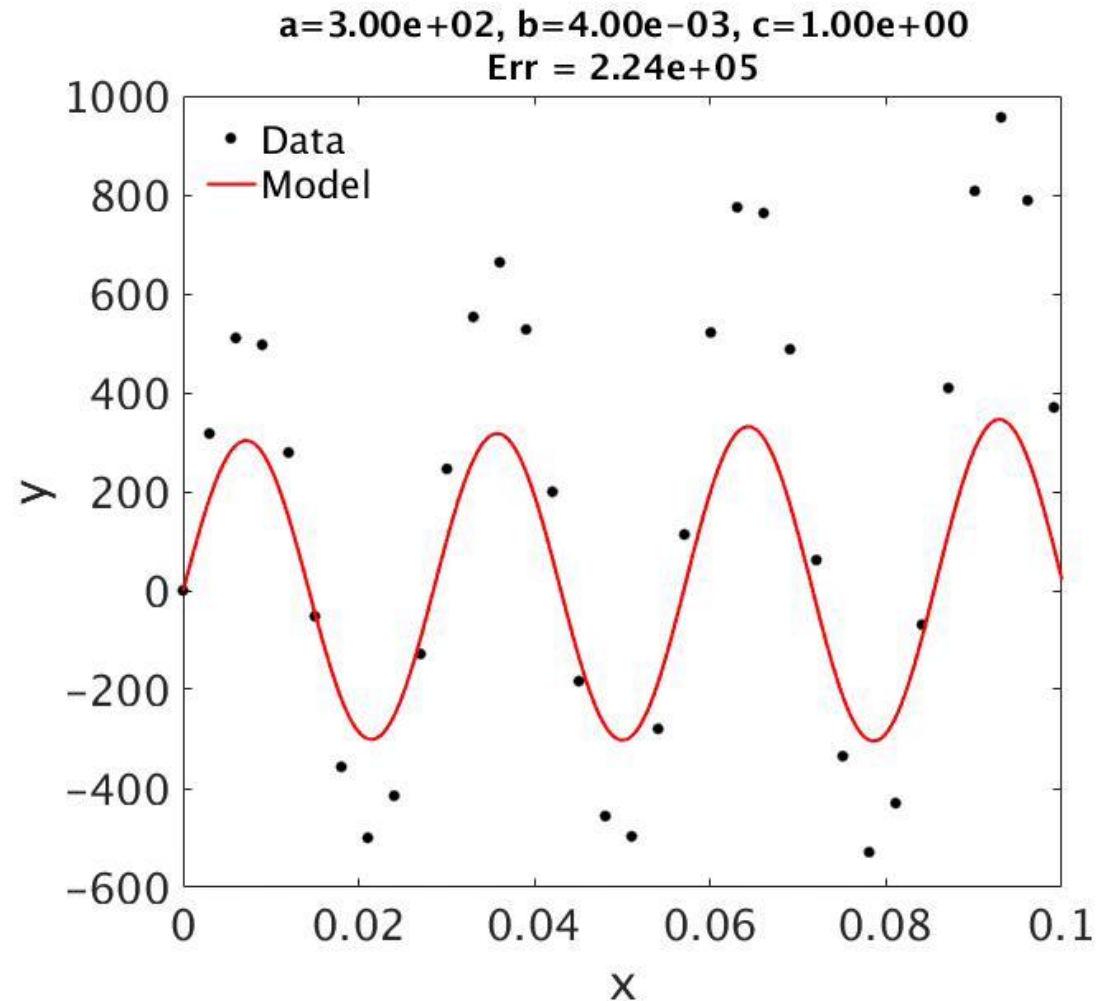
SciPy

Calibration – Methods

Gradient

- Fast Convergence
- Susceptible to local minima vs. global

Global



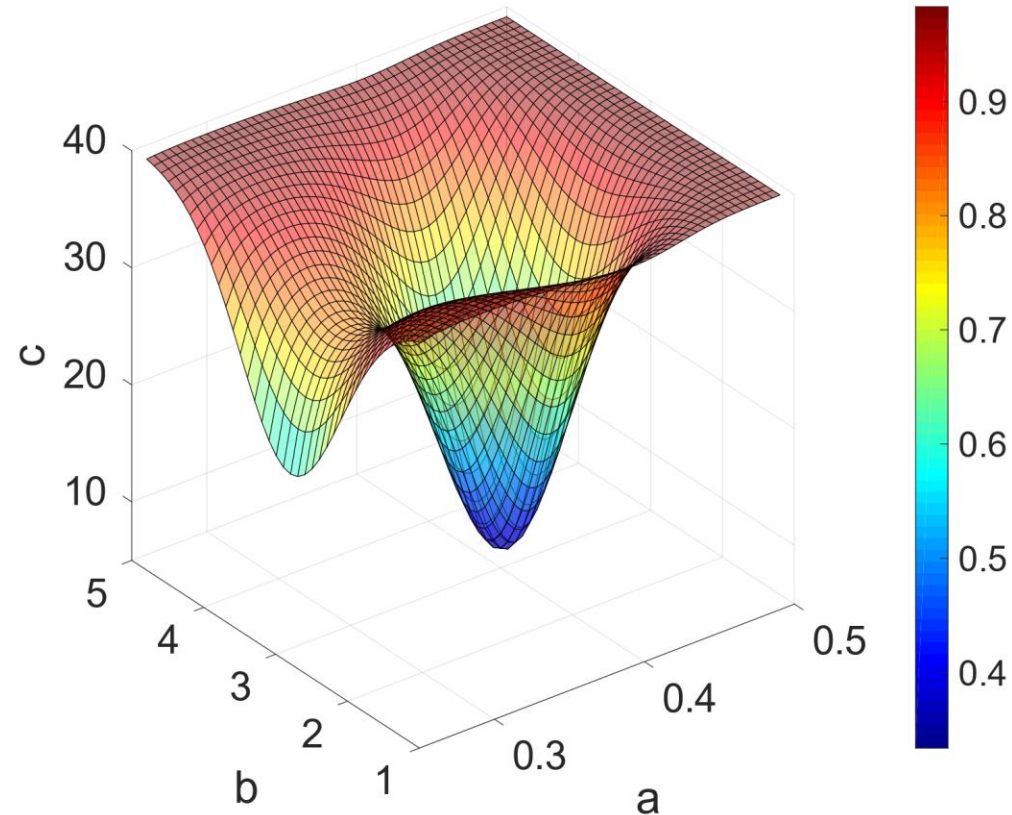
$$y = a \cdot \sin(x) \cdot \exp(bx) + cx$$

Calibration – Methods

Gradient

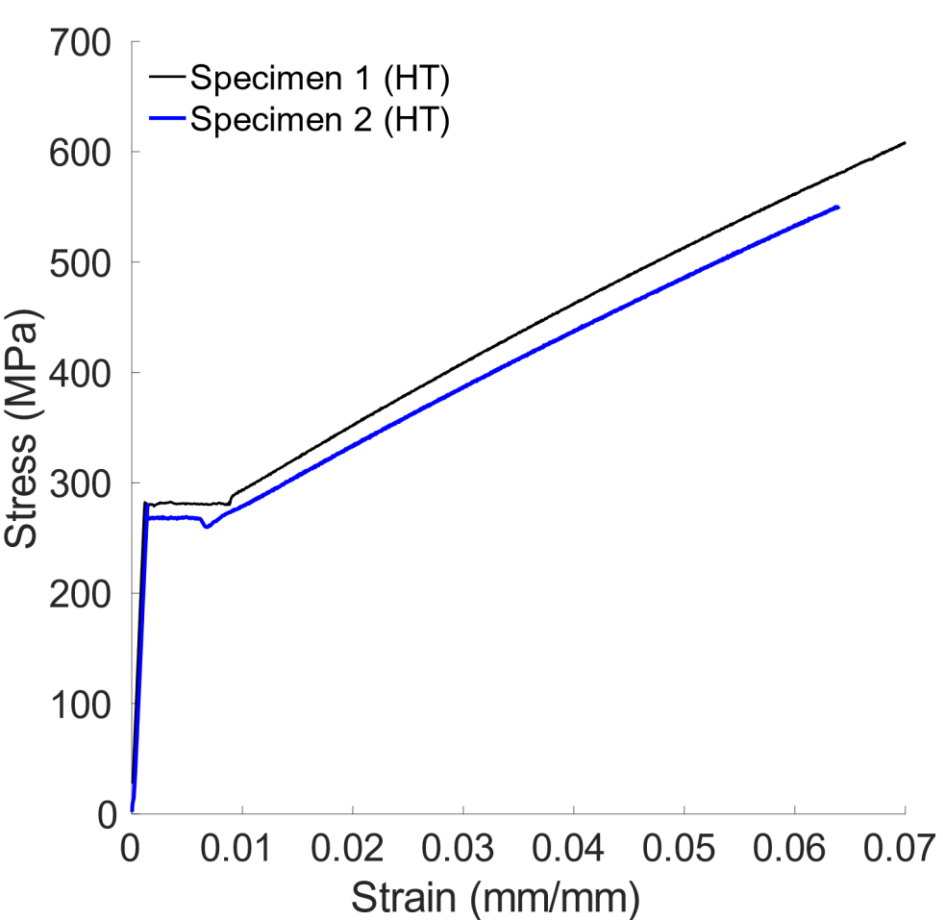
Global

- Guarantees minima
- Inefficient, can run into memory problems

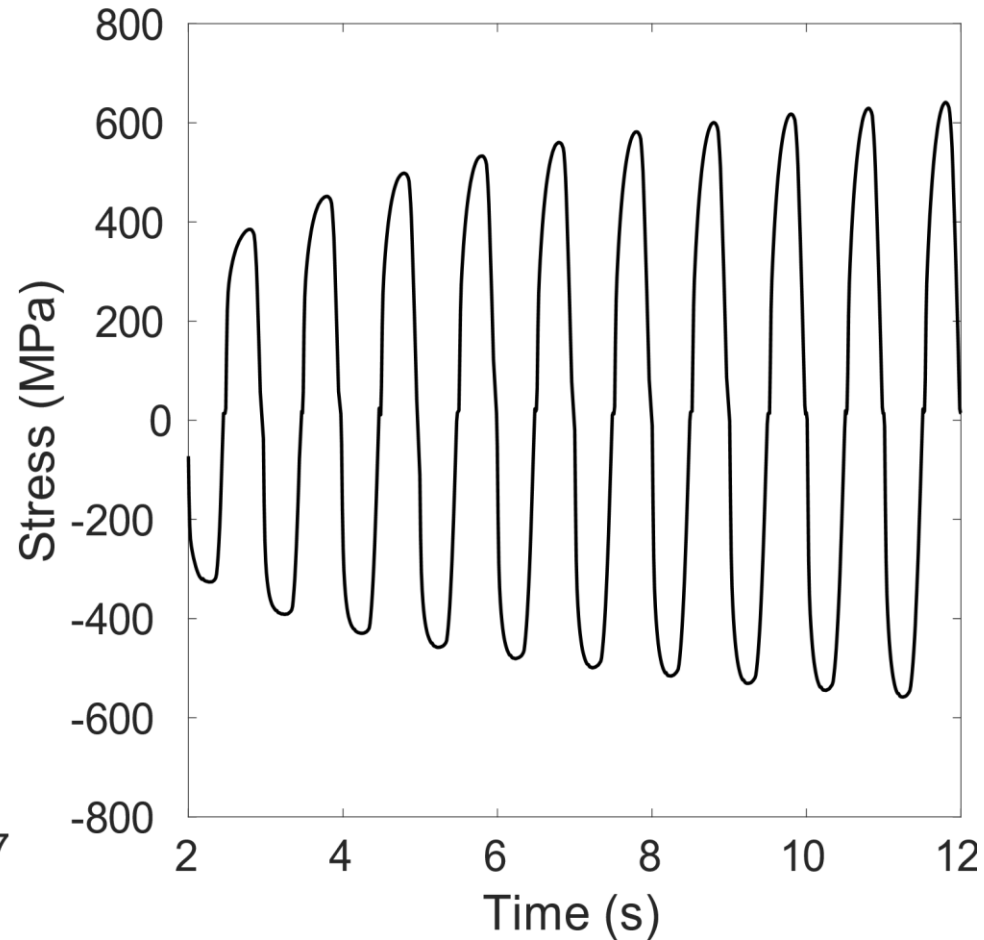


Error Function

Calibration – Data



Monotonic



Cyclic

Monotonic Calibration

J_2 Plasticity

- Generic Implementation of a von Mises yield surface with kinematic and isotropic hardening features

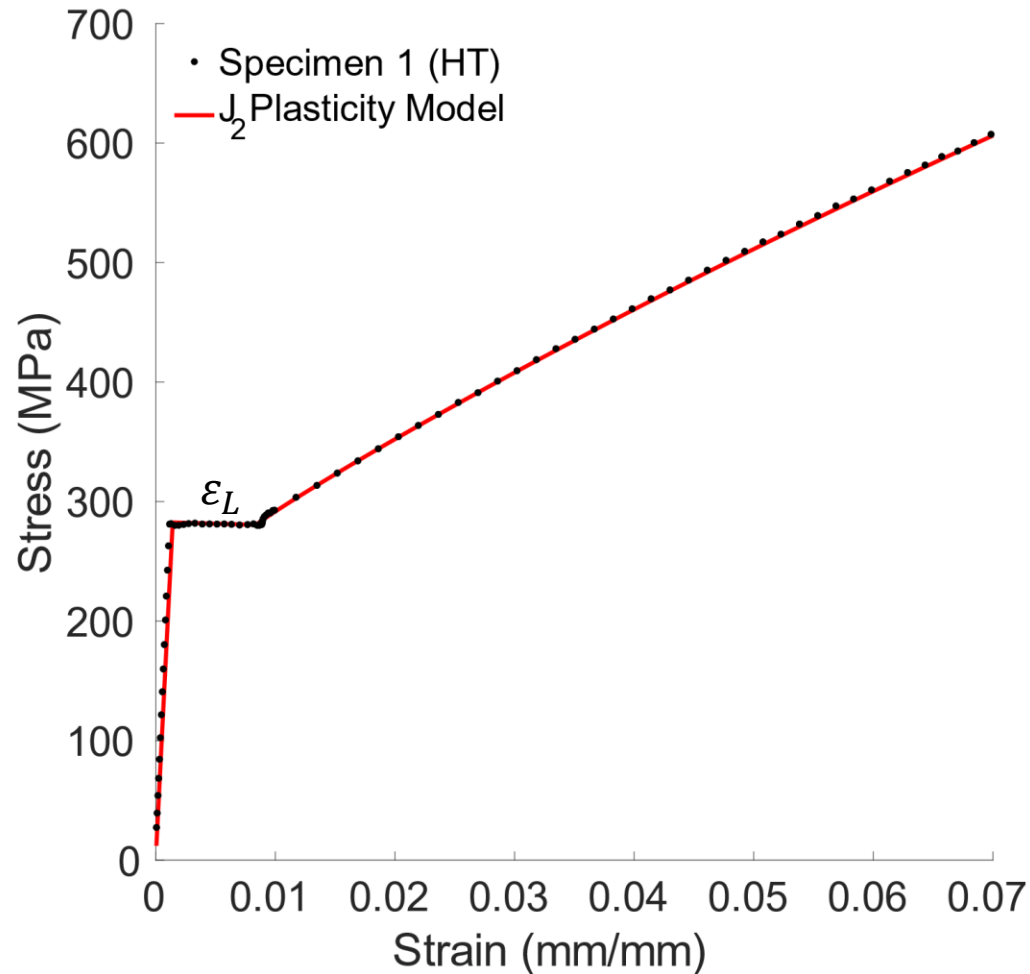
Power Law

- Describes isotropic hardening of the material

$$\bar{\sigma} = \sigma_y + A \langle \bar{\epsilon}^p - \epsilon_L \rangle^n$$

Parameters

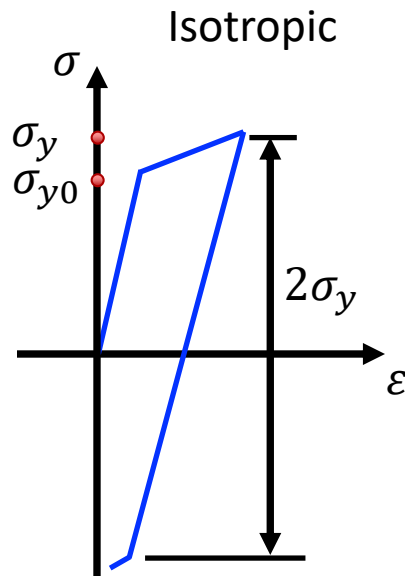
$$E, \sigma_y, \epsilon_L, \nu, n, A$$



Plastic Hardening

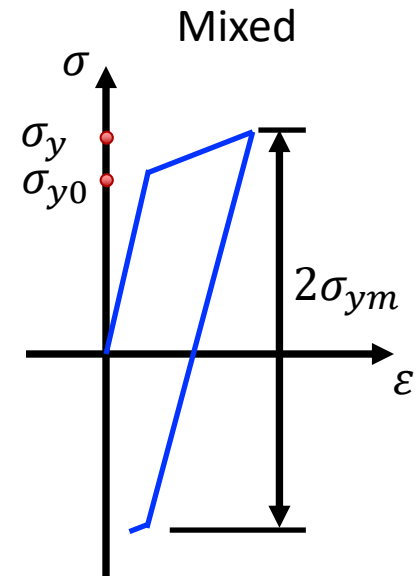
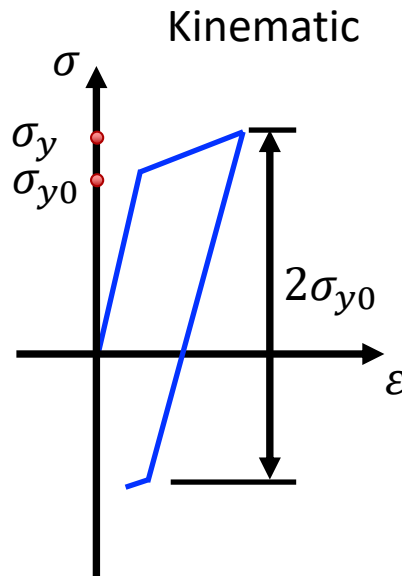
Isotropic Hardening

- Uniform shift of yield surface
- Compresses at maximum of current yield stress σ_y



Kinematic Hardening

- Asymmetry between compressive and tensile yield stress
- Bauschinger's Effect
- Max compression of initial yield stress σ_{y0}



Cyclic Calibration

BCJ_MEM

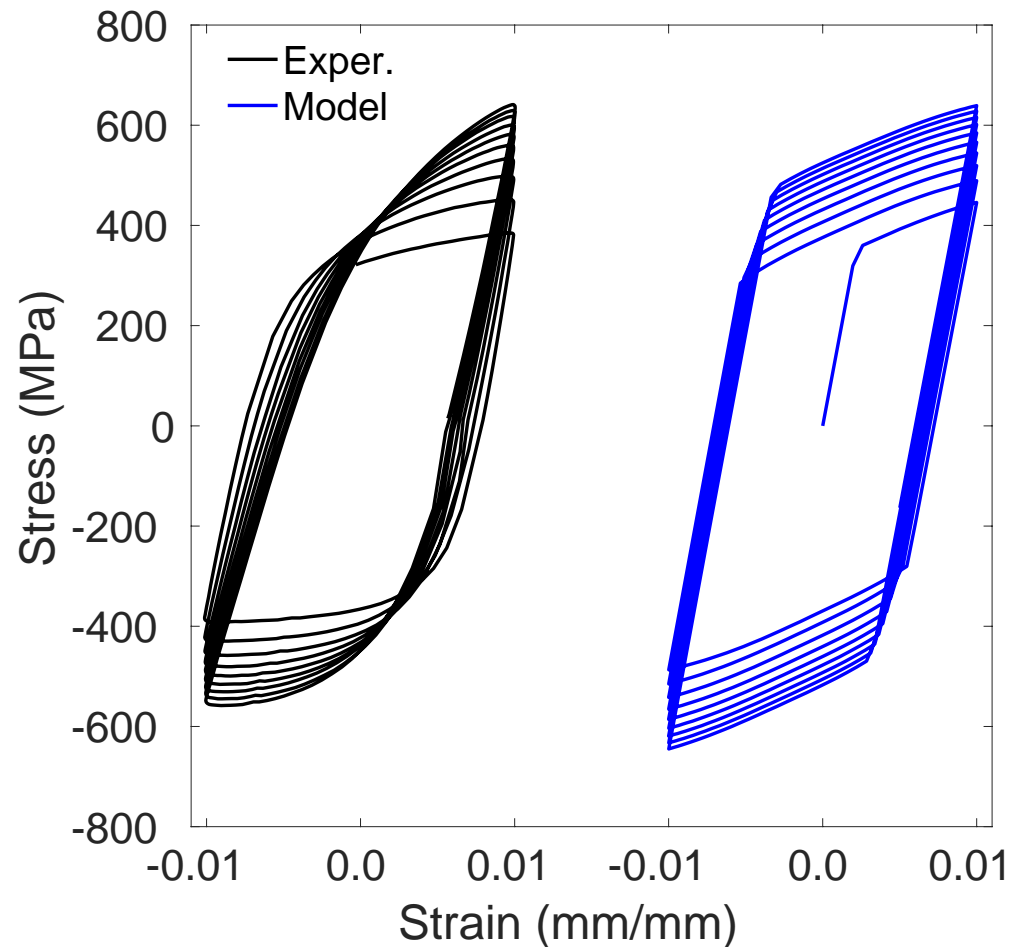
- Rate and temperature-dependent elastoviscoplasticity model with isotropic damage
- Includes effects of recrystallization and grain growth

Plastic Strain

$$\dot{\epsilon}_p = f(\theta) \sinh \left\langle \frac{\sigma}{\kappa + Y(\theta)} - 1 \right\rangle, \\ \dot{\kappa}(\kappa, H, R_{d1})$$

Parameters

$$E, \sigma_y, \nu, H_1, h_1, R_{d1}, r_{d1}$$



Cyclic Fit – 2

Ramberg-Osgood Curve

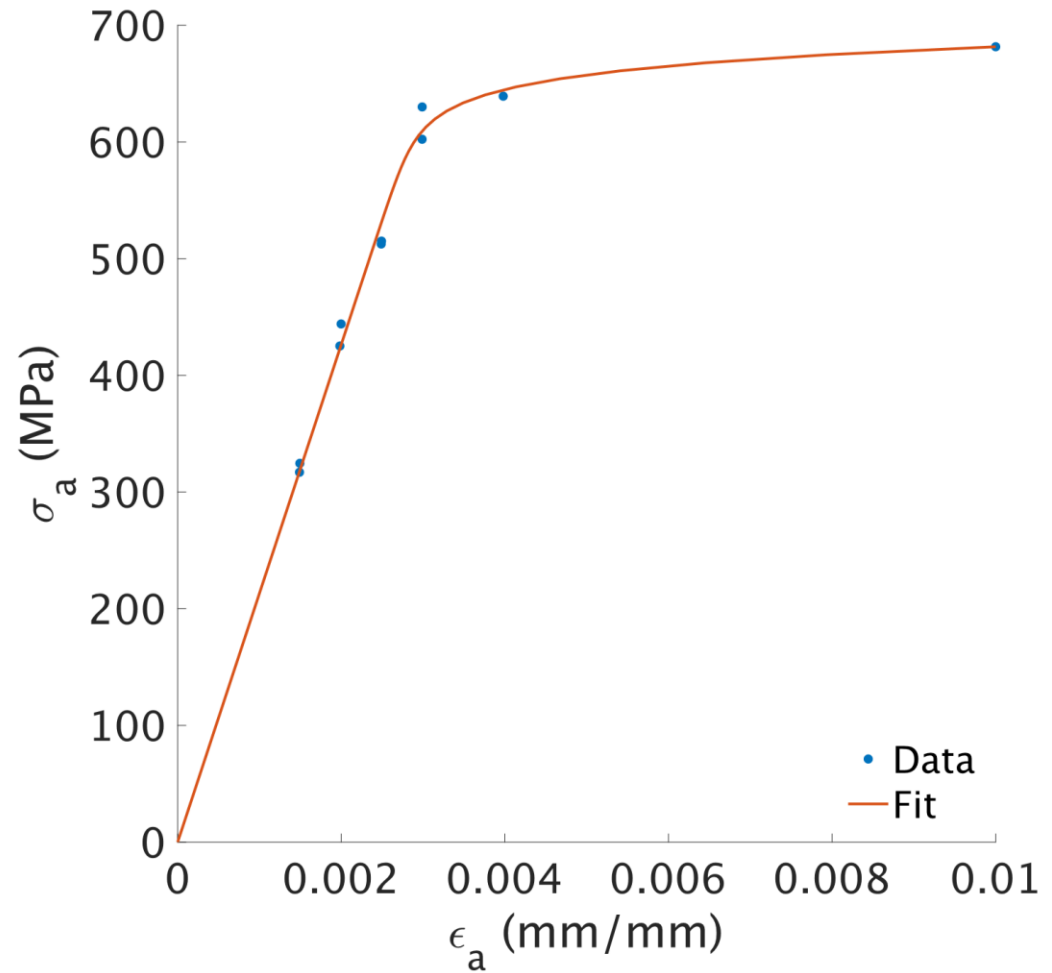
- Based on cyclic stress and strain amplitudes from near half the fatigue life
- Used to obtain n' and H' for analytical model

$$\varepsilon_a = \frac{\sigma_a}{E} + \left(\frac{\sigma_a}{H'} \right)^{n'}$$

Parameter Values:

$$n' = 0.0112$$

$$H' = 7.13 \cdot 10^{10} \text{ Pa}$$

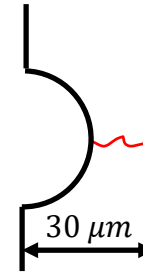


Multi-Stage Fatigue (MSF) Model

$$N_{total} = N_{INC} + N_{SC} + N_{LC}$$

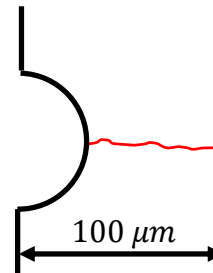
Incubation Cycles, N_{INC} :

$$\beta = \frac{\Delta\gamma_{max}^{p*}}{2} = C_{INC} N_{INC}^{\alpha}$$



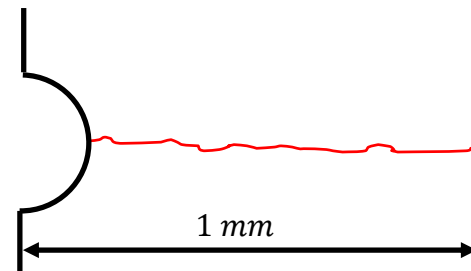
Small Crack Growth Cycles, N_{SC} :

$$\left(\frac{da}{dN}\right)_{SC} = \chi(\Delta CTOD - \Delta CTOD_{th})$$



Long Crack Growth Cycles:

$$\left(\frac{da}{dN}\right)_{LC} = \frac{C_i (\Delta K_{eff})^{n_i}}{\left[1 - \left(\frac{K_{max}}{K_{Ic}}\right)^q\right]}$$

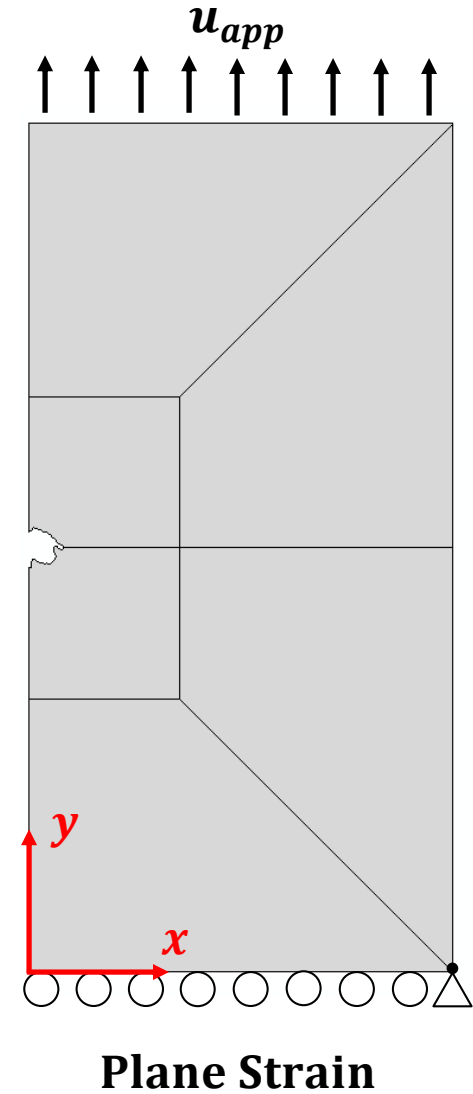
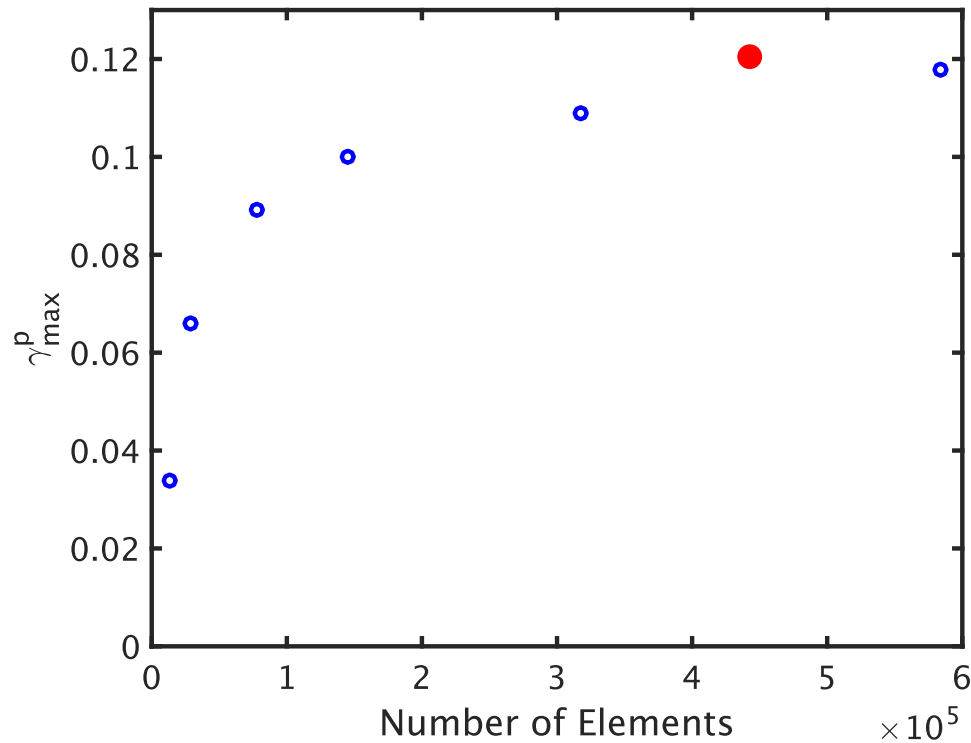
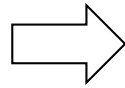
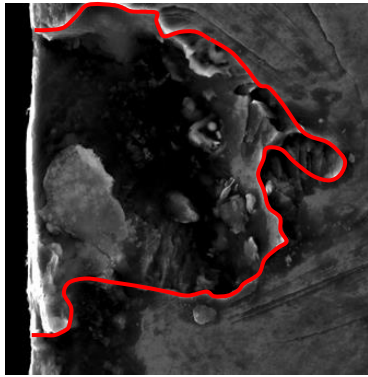


Source: McDowell et al., Eng Fract Mech, 2003

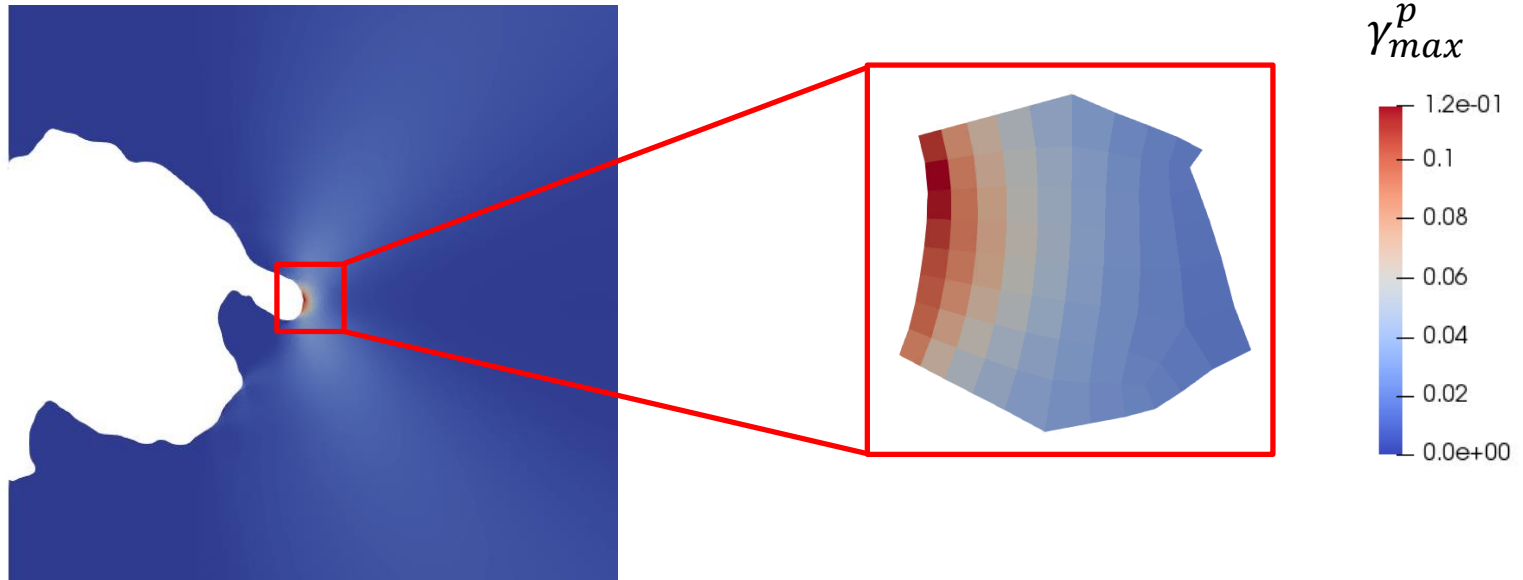
Xue et al., Eng Fract Mech, 2007

Xue et al., Acta Materialia, 2010

Finite Element Model – 2D



Average Maximum Plastic Shear Strain γ_{max}^{P*}

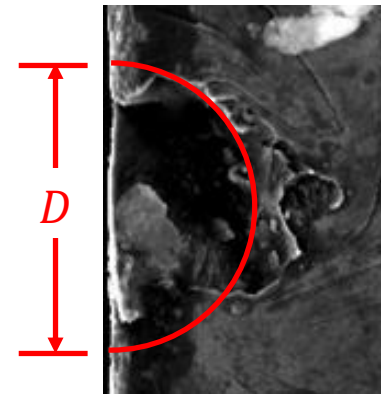


$$\gamma_{max}^{p*} = \frac{1}{A_{\beta}} \int_{A_{\beta}} \gamma_{max}^p dA$$

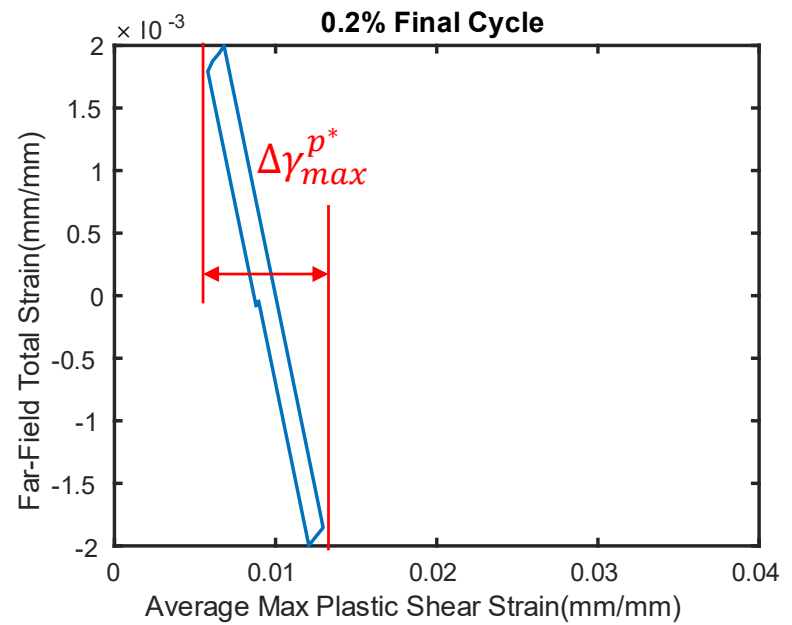
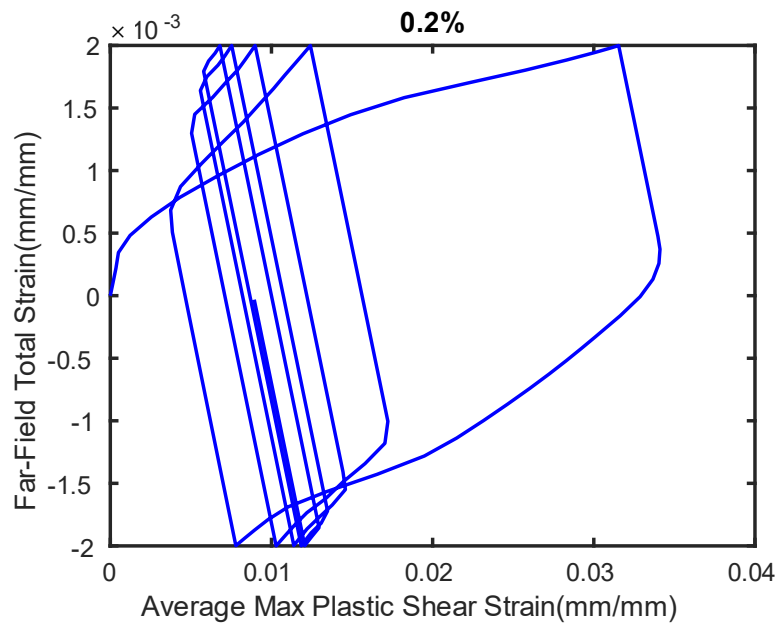
[Source: Xue et al., Eng. Fract. Mech., 2007]

$$A_{\beta} = 0.012D^2$$

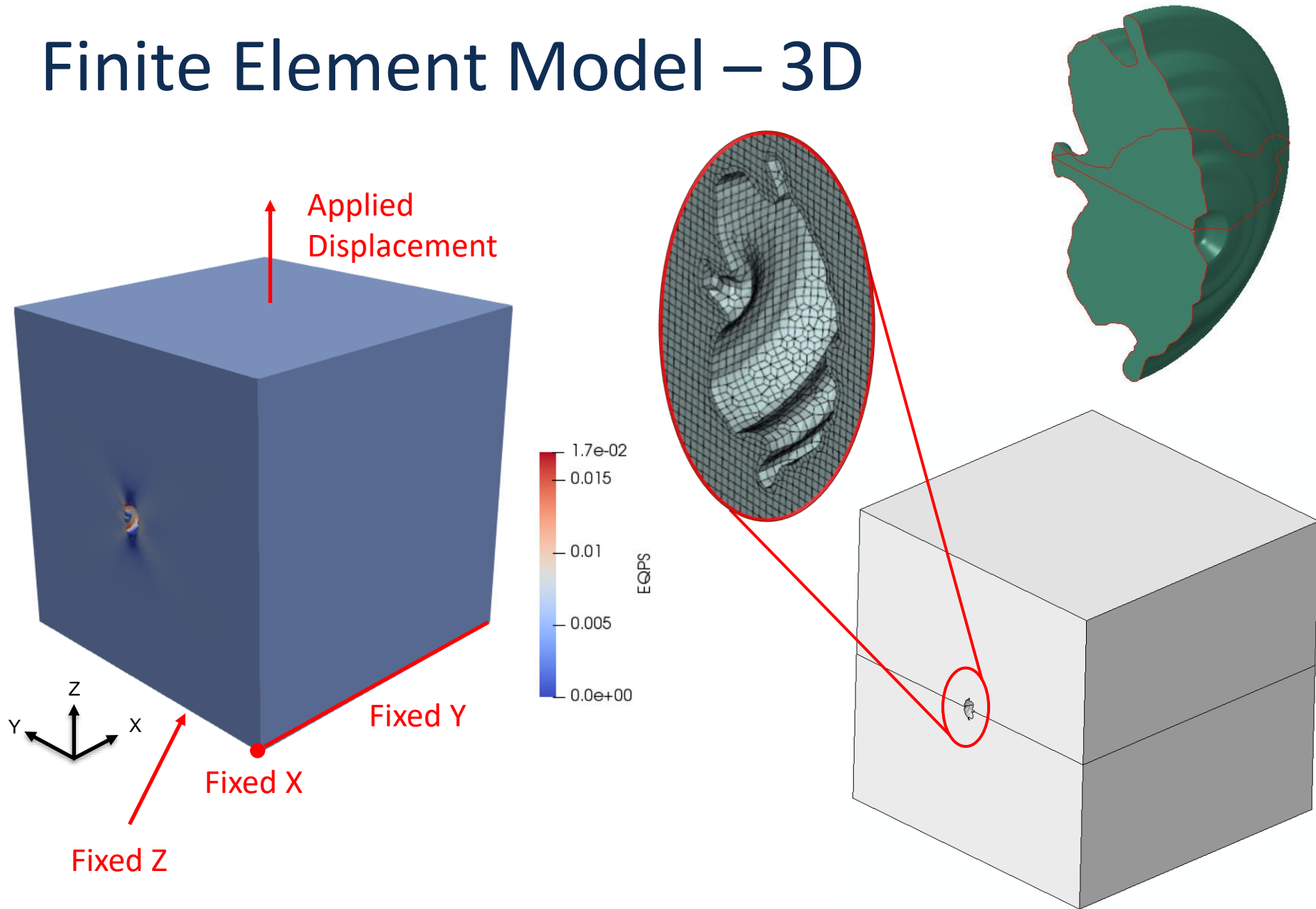
[Source: Gall et al., Int J Fract, 2001]



γ_{max}^{p*} versus ε_a

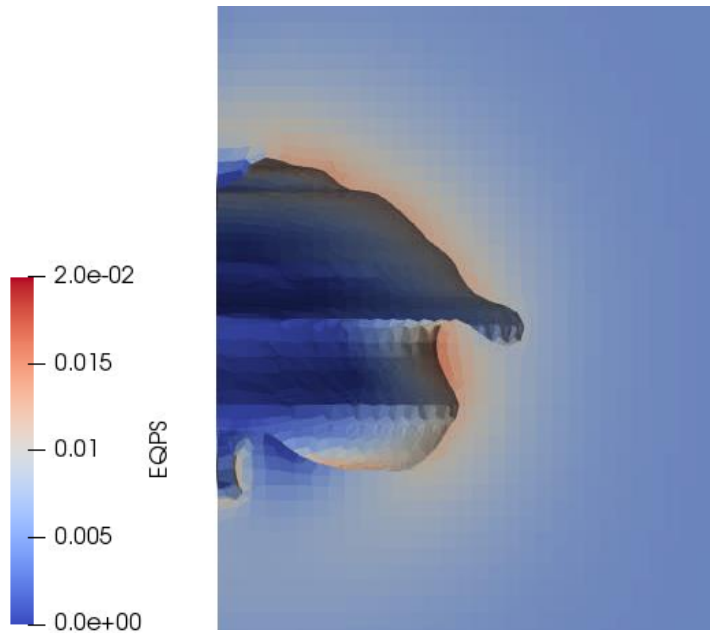


Finite Element Model – 3D

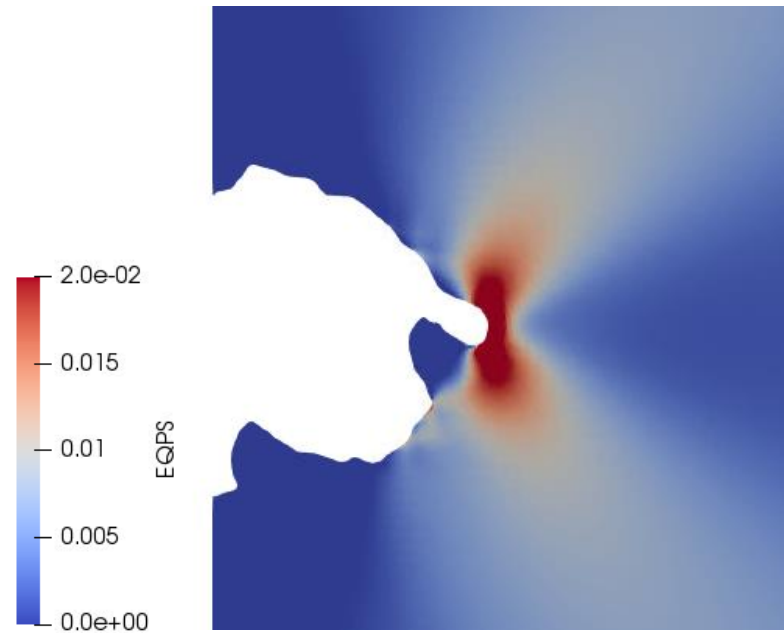


3D versus 2D

3D Model



2D Model

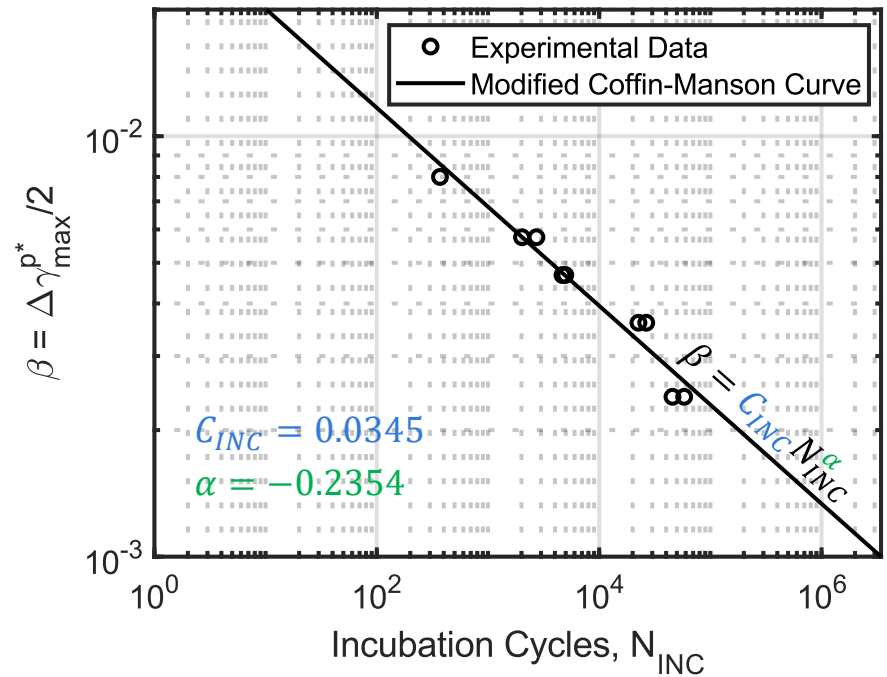
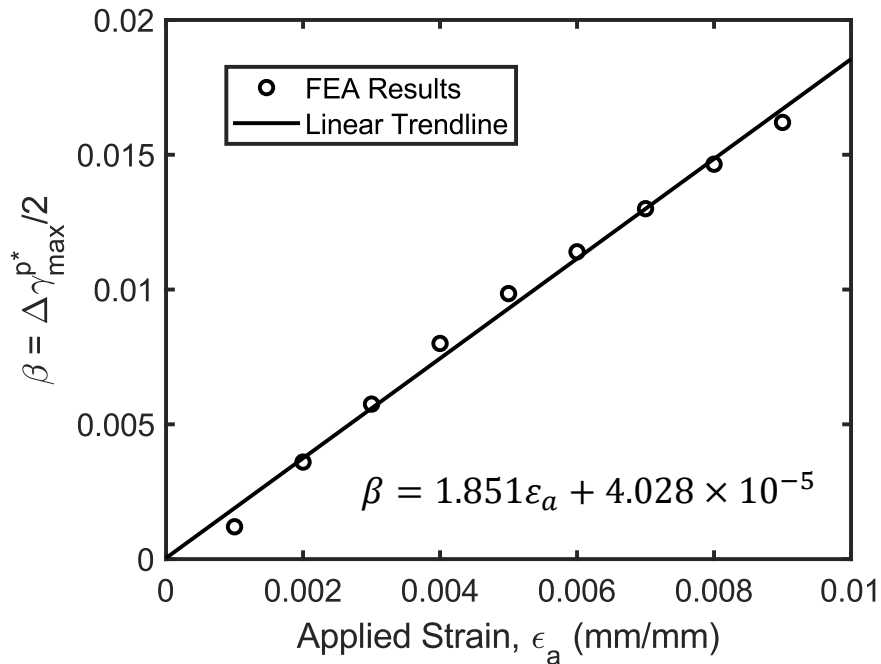


MSF Model

$$N_{total} = N_{INC} + N_{SC} + N_{LC}$$

Incubation Cycles, N_{INC} :

$$\beta = \frac{\Delta\gamma_{max}^{p*}}{2} = C_{INC} N_{INC}^{\alpha}$$

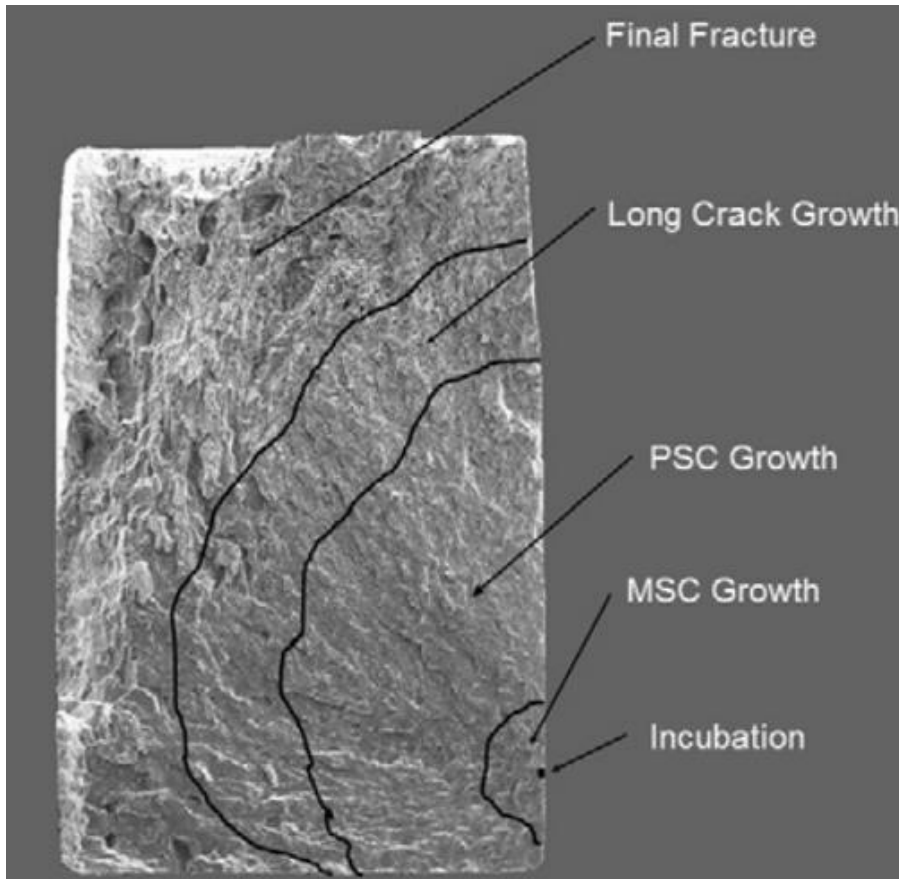


MSF Model

$$N_{total} = N_{INC} + N_{SC} + N_{LC}$$

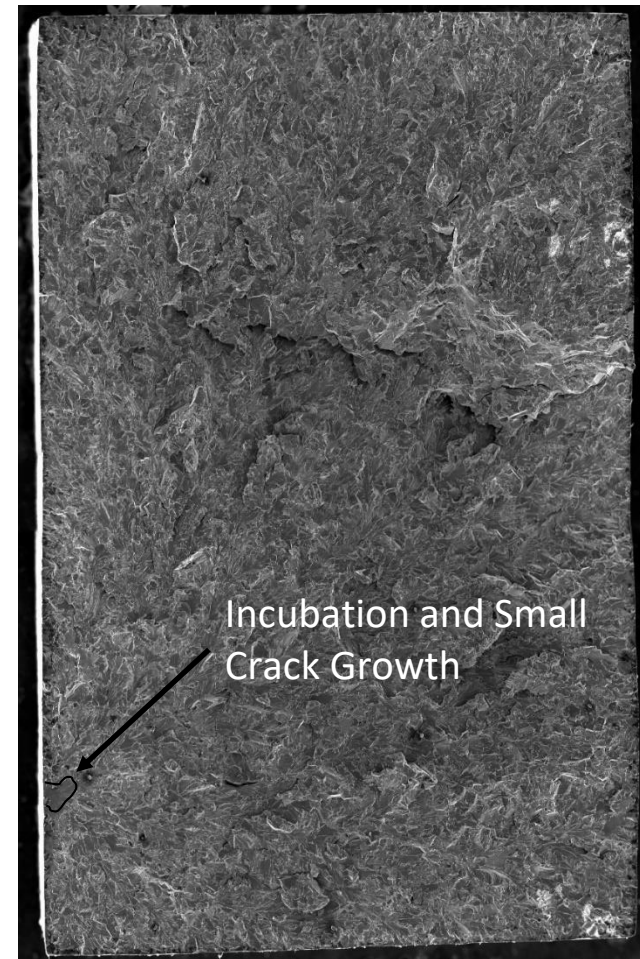
Incubation Cycles, N_{INC} :

Ti-6Al-4V



[Source: Torries et al., JOM, 2017]

Fe-Co-2V



Crack Propagation

- Crack propagation path determined using the **eXtended Finite Element Method (XFEM)**

$$u^h(x) = \sum_{I \in N} N_I(x) \left[u_I + \overbrace{H(x)a_I}^{\text{Heaviside Enrichment Term}} + \overbrace{\sum_{\alpha=1}^4 F_{\alpha} b_I^{\alpha}}^{\text{Crack Tip Enrichment Term}} \right]$$

[Source: Abaqus Analysis User's Guide, v6.14, Section 10.7]

- Initial crack: $0.01D = 0.542 \mu m$
- Propagation modeled using LEFM
- Kink angle determined using *Maximum tangential stress criterion*:

$$\hat{\theta} = \cos^{-1} \left(\frac{3K_{II}^2 + \sqrt{K_I^4 + 8K_I^2 K_{II}^2}}{K_I^2 + 9K_{II}^2} \right)$$

[Source: Abaqus Theory Guide, v6.14, Section 2.16]

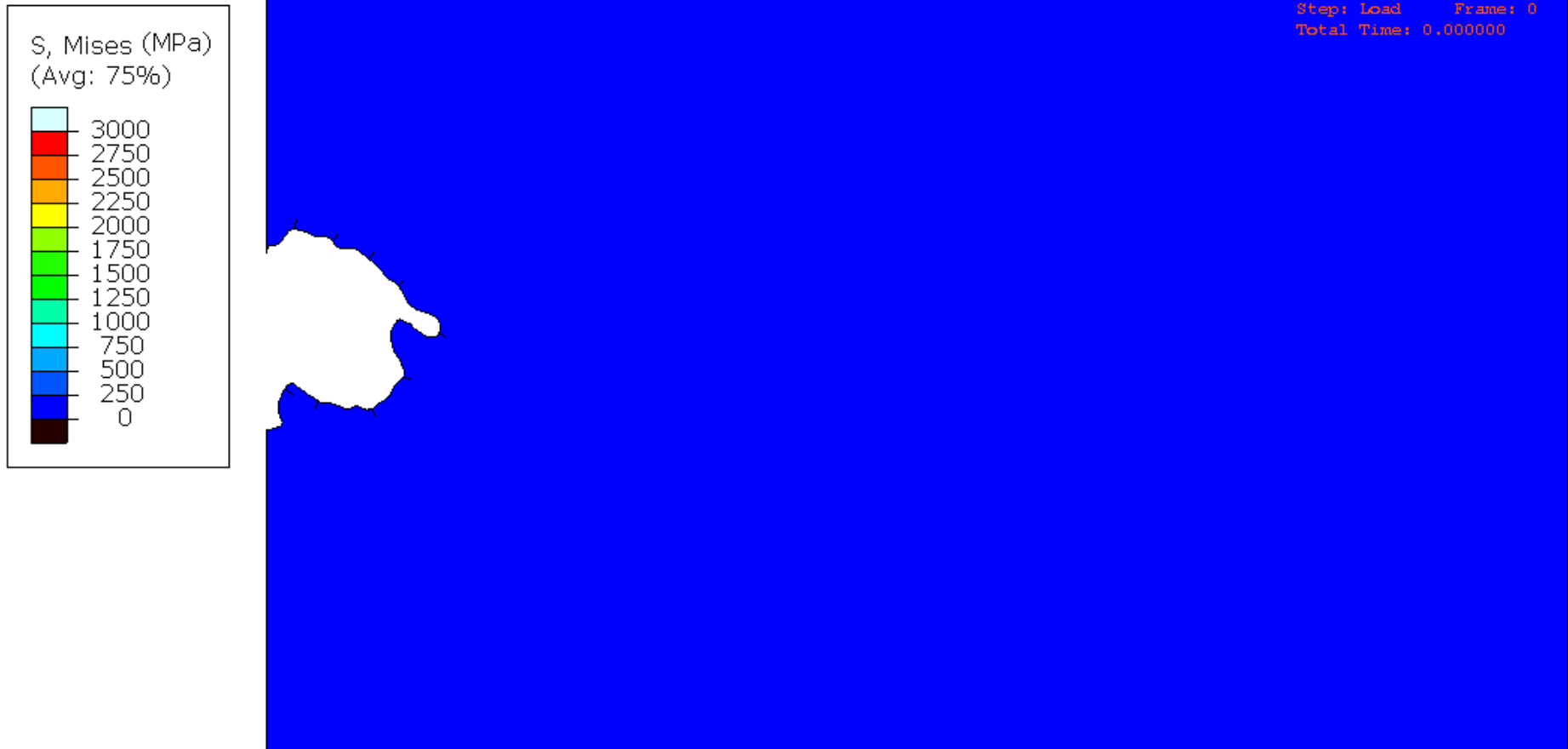
Crack Propagation

Applied Static Load

$$\varepsilon_{app} = 0.5\%$$

Linear Elastic Model

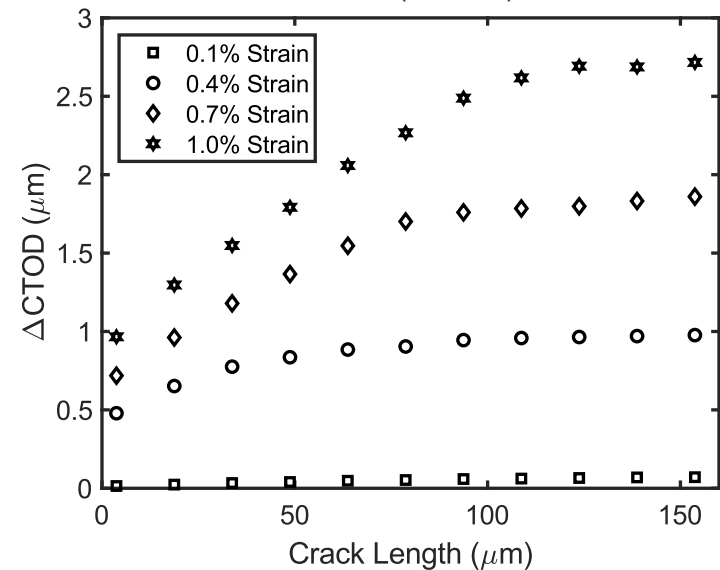
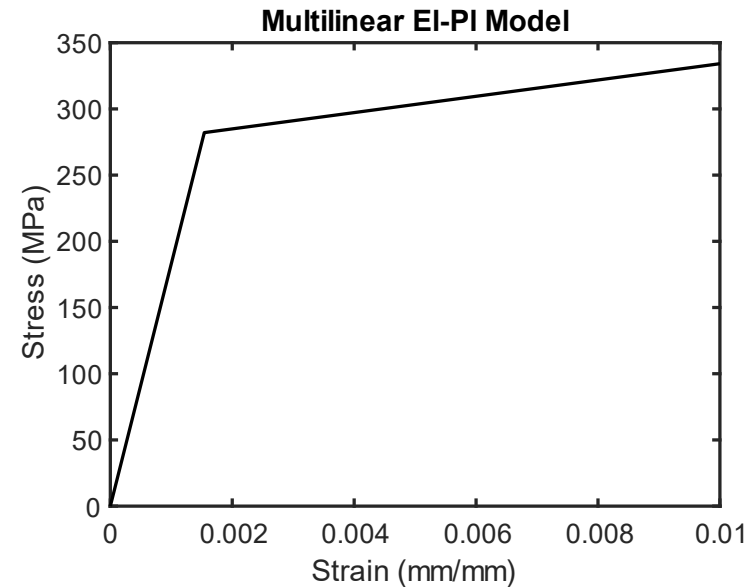
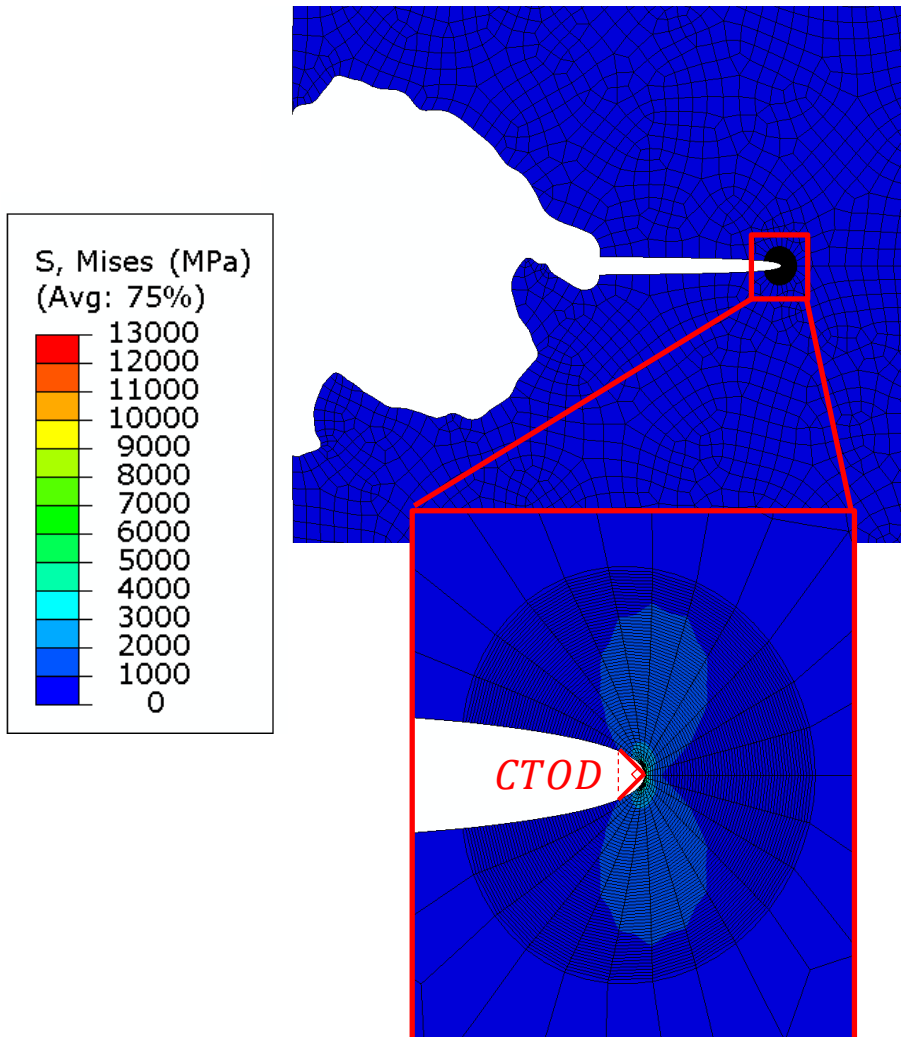
$$E = 215 \text{ MPa} , \nu = 0.335$$



MSF Model

$$N_{total} = N_{INC} + N_{SC} + N_{LC}^0$$

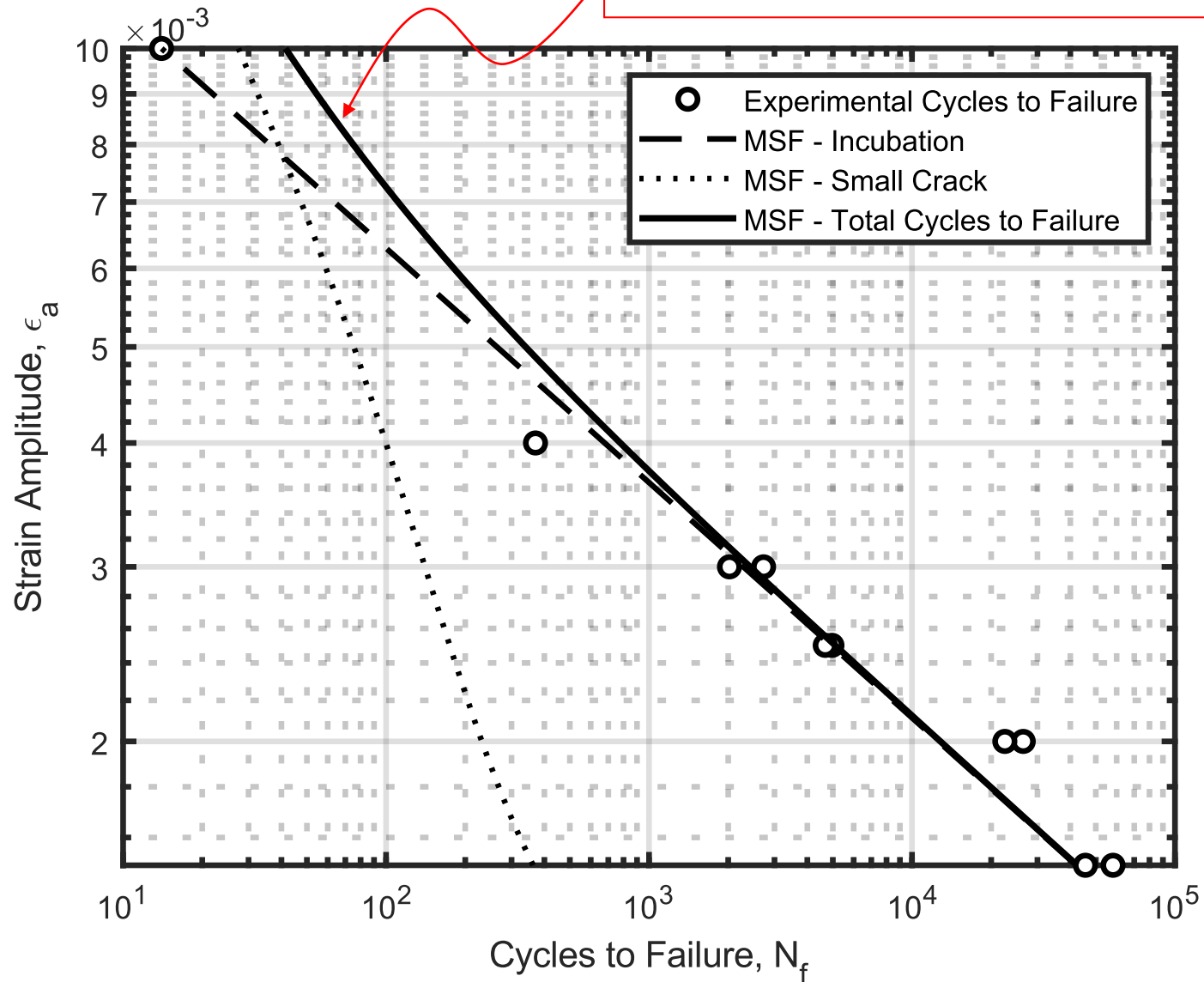
Small Crack Growth Cycles, N_{SC} :



MSF Model

Larger discrepancy between MSF prediction and experimental data for larger strain amplitudes

→ Incubation life assumption



Conclusions & Future Work

Conclusions

- Fe-Co-2V Coffin-Manson parameters σ'_f , b , ε'_f , and c determined for the first time
- Micromechanical simulations were used to compute the nonlocal maximum plastic shear strain amplitude (β) and crack tip opening displacement (CTOD)
- A Multi-Stage Fatigue model was used to predict fatigue life with no parameter calibration

Future Work

- Upper and lower defect sizes to bound MSF model prediction
- Analysis of AM CT imagery
- More fatigue tests to populate strain-life curve

Acknowledgments

- This research was conducted at the 2018 Nonlinear Mechanics and Dynamics Research Institute hosted by Sandia National Laboratories and the University of New Mexico.
- Sandia National Laboratories is a multimission laboratory managed and operated by National Technology and Engineering Solutions of Sandia, LLC., a wholly owned subsidiary of Honeywell International, Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA-0003525.